

Dividing Polynomials

$$\frac{2x^2 + x - 3}{x - 1} \Rightarrow \frac{2x + 3}{x - 1}$$

$$\begin{array}{r} x-1 \overline{) 2x^2 + x - 3} \\ \underline{2x^2 - 2x} \\ 3x - 3 \\ \underline{3x - 3} \\ 0 \end{array}$$

$$\frac{2x^2}{x} = 2x$$

$$x - (-2x) = 3x$$

$$\begin{array}{r} 233 \\ 4 \overline{) 932} \\ \underline{8} \\ 13 \\ \underline{12} \\ 12 \\ \underline{12} \\ 0 \end{array}$$

Standard long division.

The same method applies, i.e.

$$\frac{3x^3 + x^2 + 3x + 5}{x + 1} \Rightarrow \frac{3x^2 - 2x + 5}{x + 1}$$

$$\begin{array}{r} x+1 \overline{) 3x^3 + x^2 + 3x + 5} \\ \underline{3x^3 + 3x^2} \\ -2x^2 + 3x \\ \underline{-2x^2 - 2x} \\ 5x + 5 \\ \underline{5x + 5} \\ 0 \end{array}$$

$$\frac{x^2}{x} = x$$

$$+x^2 - (+3x^2) =$$

Polynomial Division

9/10/08

$$\frac{x^3 - 3x^2 + 4x - 2}{(x+1)}$$

$$\begin{array}{r}
 x^2 - 4x + 8 \\
 x+1 \overline{) x^3 - 3x^2 + 4x - 2} \\
 \underline{x^3 + x^2} \\
 -4x^2 + 4x \\
 \underline{-4x^2 - 4x} \\
 8x - 2 \\
 \underline{8x + 8} \\
 -10
 \end{array}$$

x^2
 x
 x

~~$-4x^2 + 4x$~~
 $-4x^2 + 4x$
 $= -4x$
 $(+4x) = (-4x)$
 ~~$+4x + 4x$~~
 $+4x + 4x$
 $8x$

$$= x^2 - 4x + 8 - \frac{10}{(x+1)}$$

$$\begin{array}{r}
 2x^2 + xy - y^2 \\
 x+y \overline{) 2x^2 + xy - y^2} \\
 \underline{2x^2 + 2xy} \\
 -xy - y^2 \\
 \underline{-xy - y^2} \\
 0
 \end{array}$$

(2x - y)

$$\begin{array}{r}
 x^2 - xy + y^2 \\
 x+y \overline{) x^3 + 0x^2y + 0xy^2 + y^3} \\
 \underline{x^3 + x^2y} \\
 -x^2y + 0xy^2 \\
 \underline{-x^2y - xy^2} \\
 xy^2 + y^3 \\
 \underline{xy^2 + y^3} \\
 0
 \end{array}$$

(0xy - (-xy))

$$\frac{6x^2 + 7x - 5}{x - 1}$$

$$x \times x = x^2$$

$$x-1 \overline{) \begin{array}{r} 6x \\ 6x^2 + 7x - 5 \\ \underline{6x^2 - 6x} \end{array}}$$

$$\frac{6x^2 + 7x}{x}$$

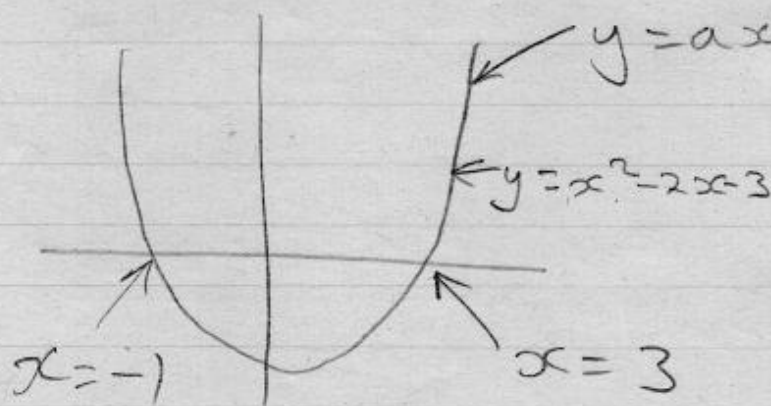
$$7x$$

$$x-1 \overline{) \begin{array}{r} 6x + 13 + \frac{8}{x-1} \\ 6x^2 + 7x - 5 \\ \underline{6x^2 - 6x} \\ 13x - 5 \\ \underline{13x - 13} \\ 8 \end{array}}$$

$$x-1 \overline{) \begin{array}{r} 6x + 13 \\ 6x^2 + 7x - 5 \\ \underline{6x^2 - 6x} \\ 13x - 5 \\ \underline{13x - 13} \\ 8 \end{array}}$$

FACTOR | HERON

linear $y = mx + c$
quadratic $y = ax^2 + bx + c$



$$x \times x = x^2 + 1x - 3$$

$$(x+1)(x-3) = 0$$

$$x^2 - 2x - 3 = 0$$

$$\therefore x + 1 = 0$$

$$\therefore x - 3 = 0$$

$$x^3 - 2x^2 - 5x + 6 = 0$$

$$\cancel{A} \quad (x-1)(x^2 - x - 6) = 0$$

	x^3	$-2x^2$	$-5x$	$+6$	$= 0$
$f(1)$	1	-2	-5	+6	= 0

$$\begin{array}{r}
 x^2 - x - 6 \\
 \hline
 x-1 \overline{) x^3 - 2x^2 - 5x + 6} \\
 \underline{x^3 - x^2} \\
 -x^2 - 5x \\
 \underline{-x^2 + x} \\
 -6x + 6 \\
 \underline{-6x + 6} \\
 0
 \end{array}$$

$$\begin{aligned}
 x^2 &= (x \times x^3) \\
 -x^2 &= (x^2 \times -1)
 \end{aligned}$$

$$\begin{aligned}
 &(-2x^2 - (-x^2)) \\
 &(-x \times x) \\
 & \\
 &(-6x \times x) \\
 &
 \end{aligned}$$

$$-5 - (1) = -6$$

REMAINDER THEOREM
FIND THE REMAINDER OF...

$$\begin{array}{r}
 3x^2 - 4x + 2 \\
 \hline
 x - 2
 \end{array}$$

$$\begin{aligned}
 f(2) &= 3 \times 2^2 - 4 \times 2 + 2 \\
 &= 12 - 8 + 2 = \underline{6} \\
 \text{Remainder is } &\frac{6}{x-2}
 \end{aligned}$$

$$\begin{array}{r}
 3x + 2 \\
 \hline
 x-2 \overline{) 3x^2 - 4x + 2} \\
 \underline{3x^2 - 6x} \\
 2x + 2 \\
 \underline{2x - 4} \\
 6
 \end{array}$$

EX/

$$ax^3 + bx^2 + cx + d = 0$$

In the equation above, a, b, c and d are constants.
If the equation has roots $-1, -3$ and 5 , which of the following is a factor of $ax^3 + bx^2 + cx + d$?

- a) $x-1$
- b) $x+1$
- c) $x-3$
- d) $x+5$

Roots of an equation are values of x which when plugged into equation $ax^3 + bx^2 + cx + d$ gives you 0 as a result.

$-1, -3$ and 5 are given as roots, so $x+1, x+3$ and $x-5$ should be factors.

Its form is $x-a$ where a is the root, therefore, it implies $x=-1, x=-3$ and $x=5$, or $x+1=0, x+3=0$ and $x-5=0$ are factors of the equation.

\therefore the answer is b: $x+1$

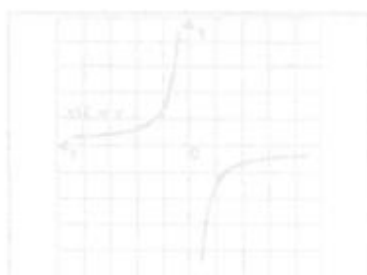
Check: $x=-1 \therefore x+1=0 \rightarrow -1+1=0 \checkmark$
 $x=-3 \therefore x+3=0 \rightarrow -3+3=0 \checkmark$
 $x=+5 \therefore x-5=0 \rightarrow 5-5=0 \checkmark$

Types of function	General form	Highest power of variable x	Shape of the function
Linear	$y = ax + b$	1	/ or \
Quadratic	$y = ax^2 + bx + c$	2	∪ or ∩
Cubic	$y = ax^3 + bx^2 + cx + d$	3	∩ or ∪
Reciprocal	$y = \frac{a}{x}$	-1	∩ or ∪

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Polynomial Functions

Degree	Name	Example
0	Constant	5
1	Linear	$2x + 3$
2	Quadratic	$x^2 - x + 5$
3	Cubic	$3x^3 + 23$
4	Quartic	$x^4 + 2x^3 - 3$
5	Quintic	$x^5 + 2x^3 - .5x + 3$

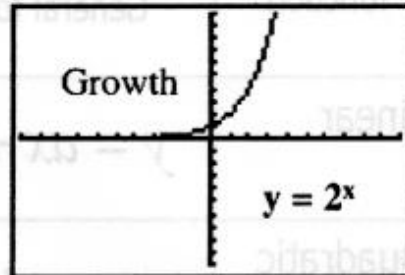


Reciprocal function

Exponential Functions

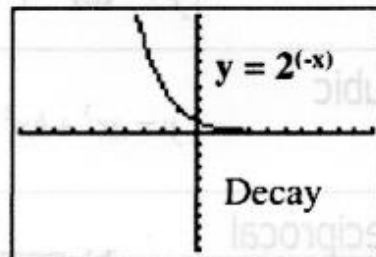
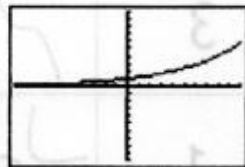
$$y = a^x$$

The independent variable (x) is found in the exponent of the function



Example

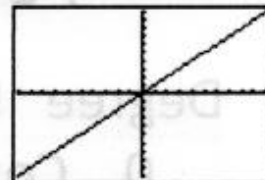
What does the graph of $y = 2^{(25x)}$ look like?



Families of Functions

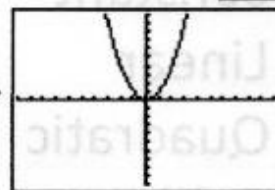
$$y = x$$

Linear function (Line)



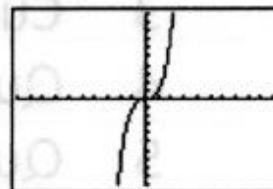
$$y = x^2$$

Quadratic Function (Parabola)



$$y = x^3$$

Cubic Function



$$y = 1/x$$

Reciprocal function

